

Challenges in Waveform Modeling with 3G Detectors

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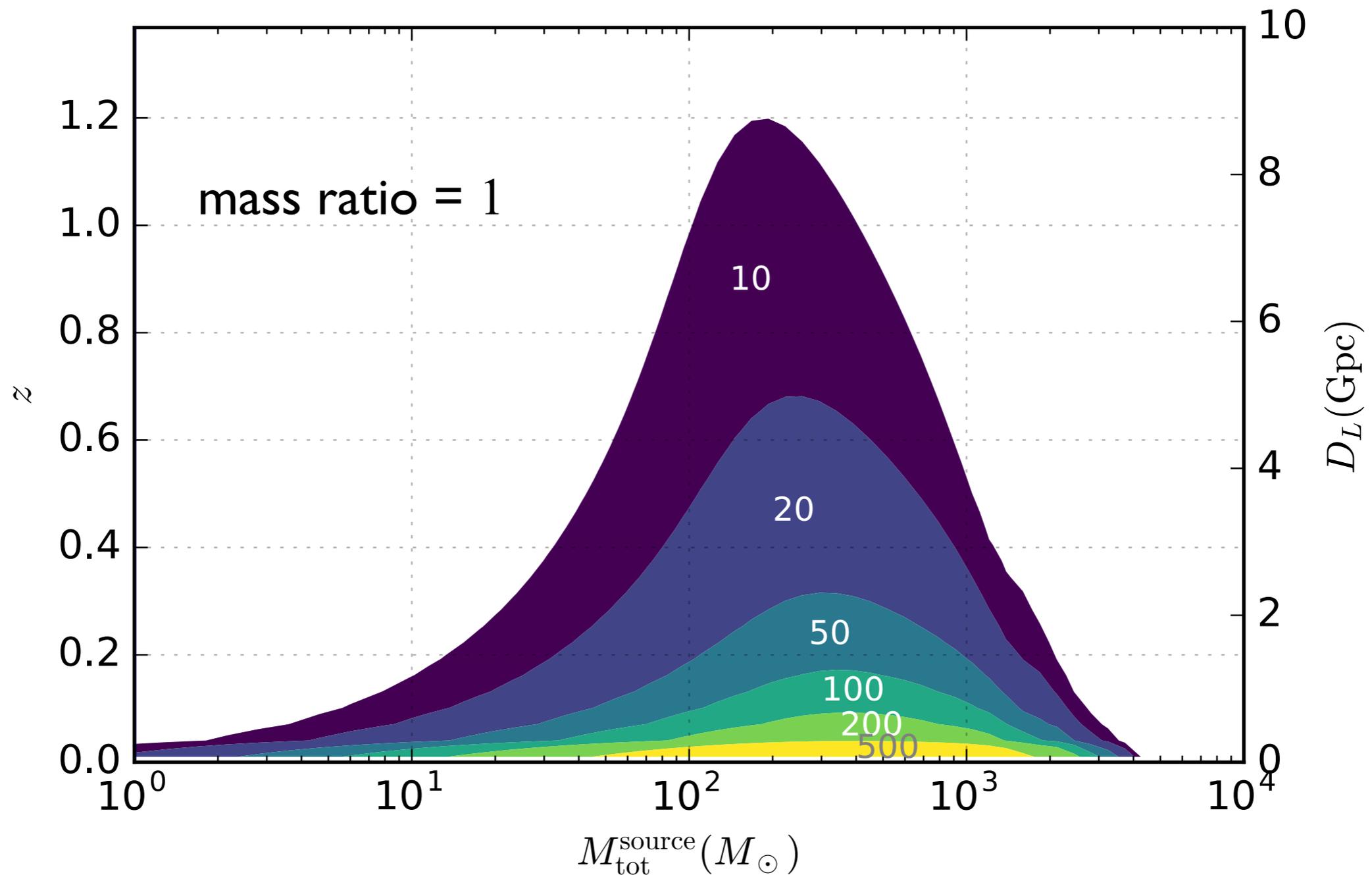


for “**Extreme Gravity & Fundamental Physics/Waveform Models**”
Working Groups

The making of 3G report of XG & Fund. Physics/WM Groups

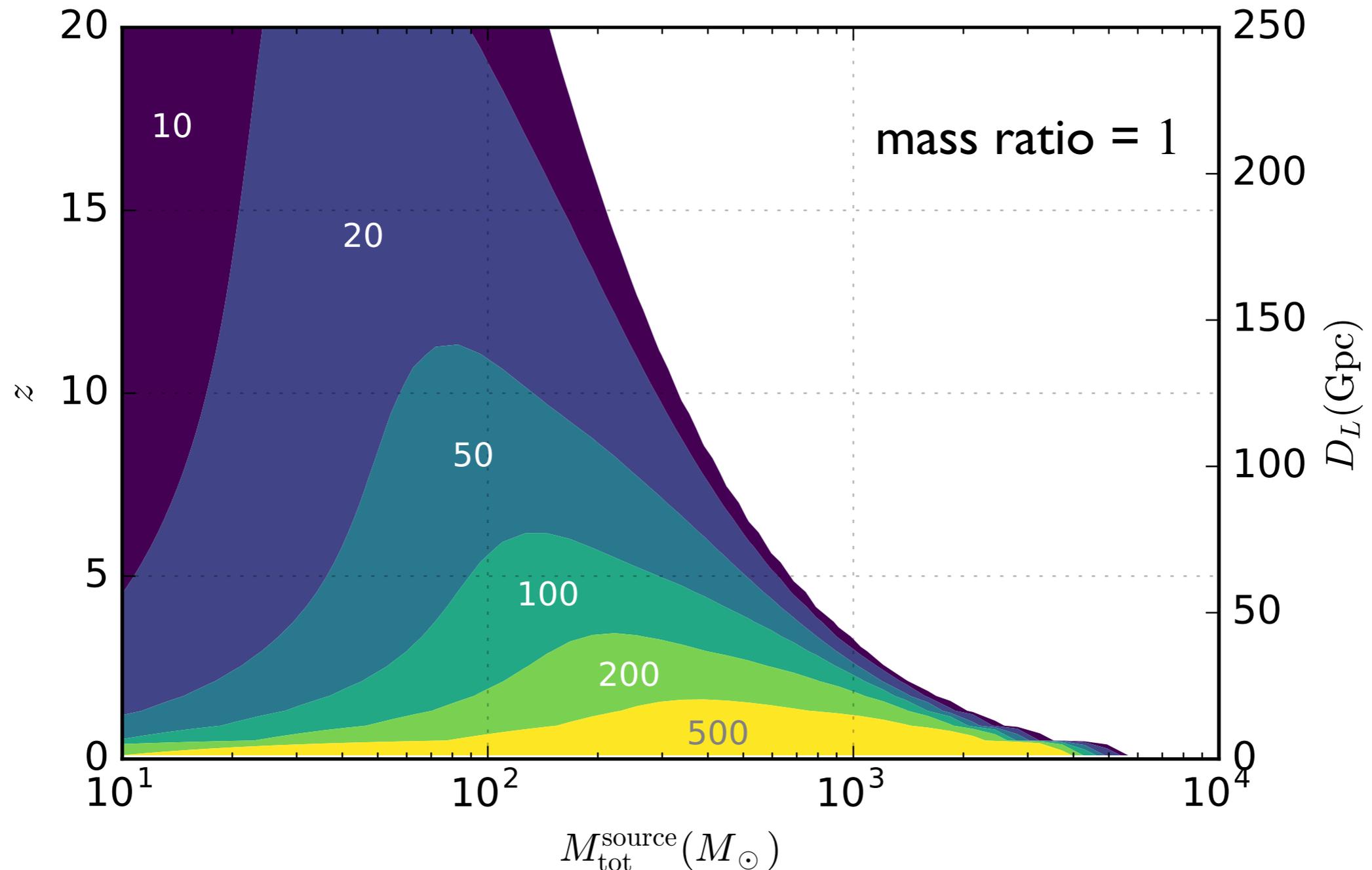
- **Four subgroups** were **formed** with contact persons:
 - Fundamental questions in gravity and particle physics (*Chatziioannou & Sotiriou*)
 - Extreme matter (*Vitale & Yunes*)
 - Exotic objects and phenomena (*Archisman & Pani*)
 - Waveform modeling and data-analysis challenges (*Ajith & Pürrer*)
- **Preliminary draft** produced in late June.
- Co-chairs *Buonanno, Lehner & van den Broeck* worked on preliminary draft and produced **first revised version of 3G report** on Sep 28
[<https://github.com/gwic-3g/3g-science-case/blob/master/work-space/xg/XG-WM-report-v1.pdf>]
- So far, several **people have contributed to 3G** report, including *Arun, Barausse, Baryakhtar, Brito, Dietrich, East, Gerosa, Harry, Hinderer, Maselli, Pfeiffer, Pratten, Shao, Tamanini, van de Meent, Varma, Vines, Zumalacarregui, Yang, ...*

Binary's masses/distance spanned by 2G detectors



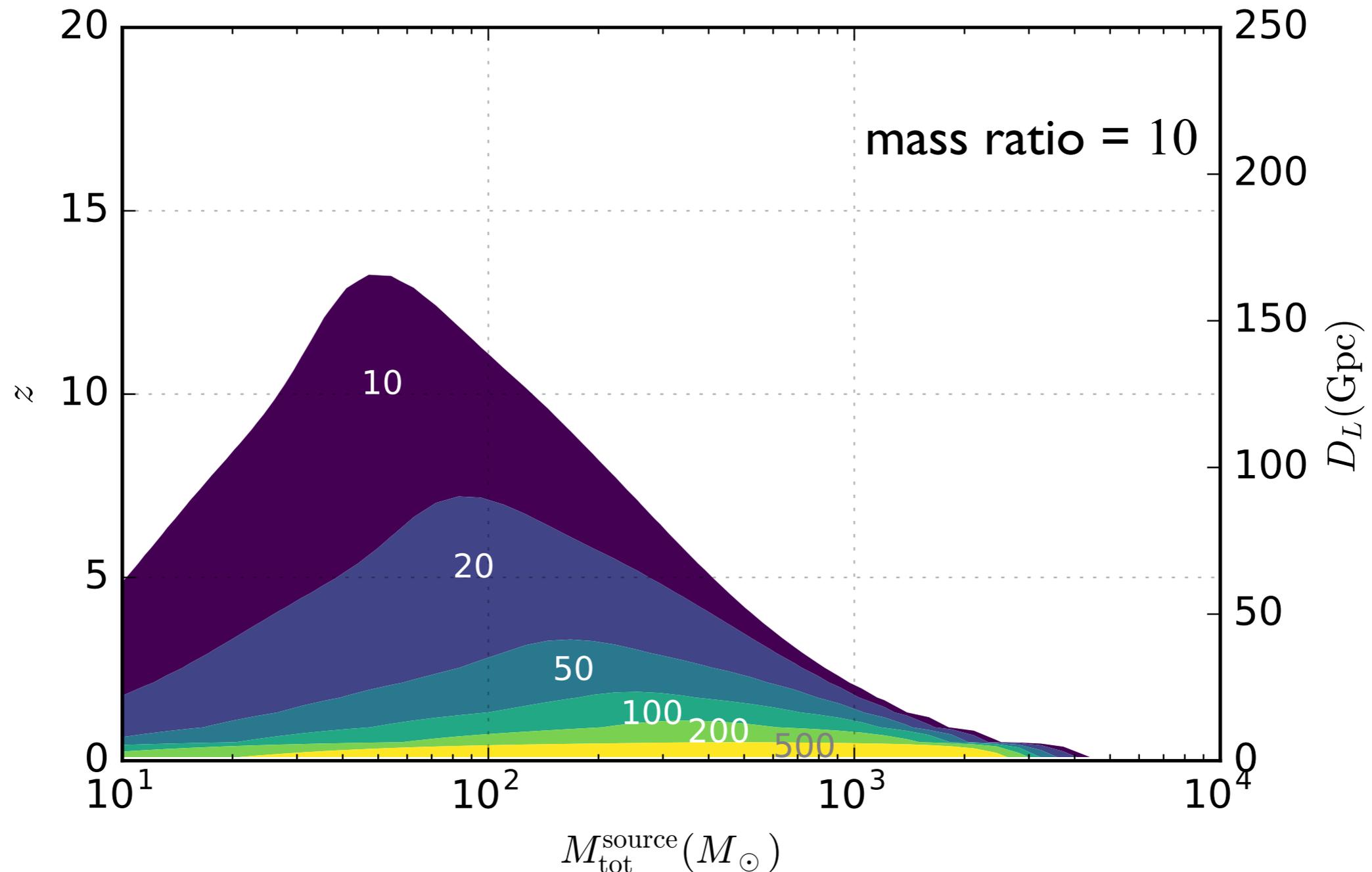
- 2G detectors will observe **binary coalescences with SNR** (~ 20) **at modest redshift** ($z \sim 0.7$), and $\text{SNR} > 100$ at $z < 0.2$.

Binary's masses/distance spanned by 3G detectors



- 3G detectors will observe **binary coalescences with SNR** (~ 20) even **at high redshift** ($z \sim 10-15$), and with **SNR** > 100 at $z < 5$.
- Demands on waveform **accuracy** are **higher**, modeling is more **challenging**.

Binary's masses/distance spanned by 3G detectors

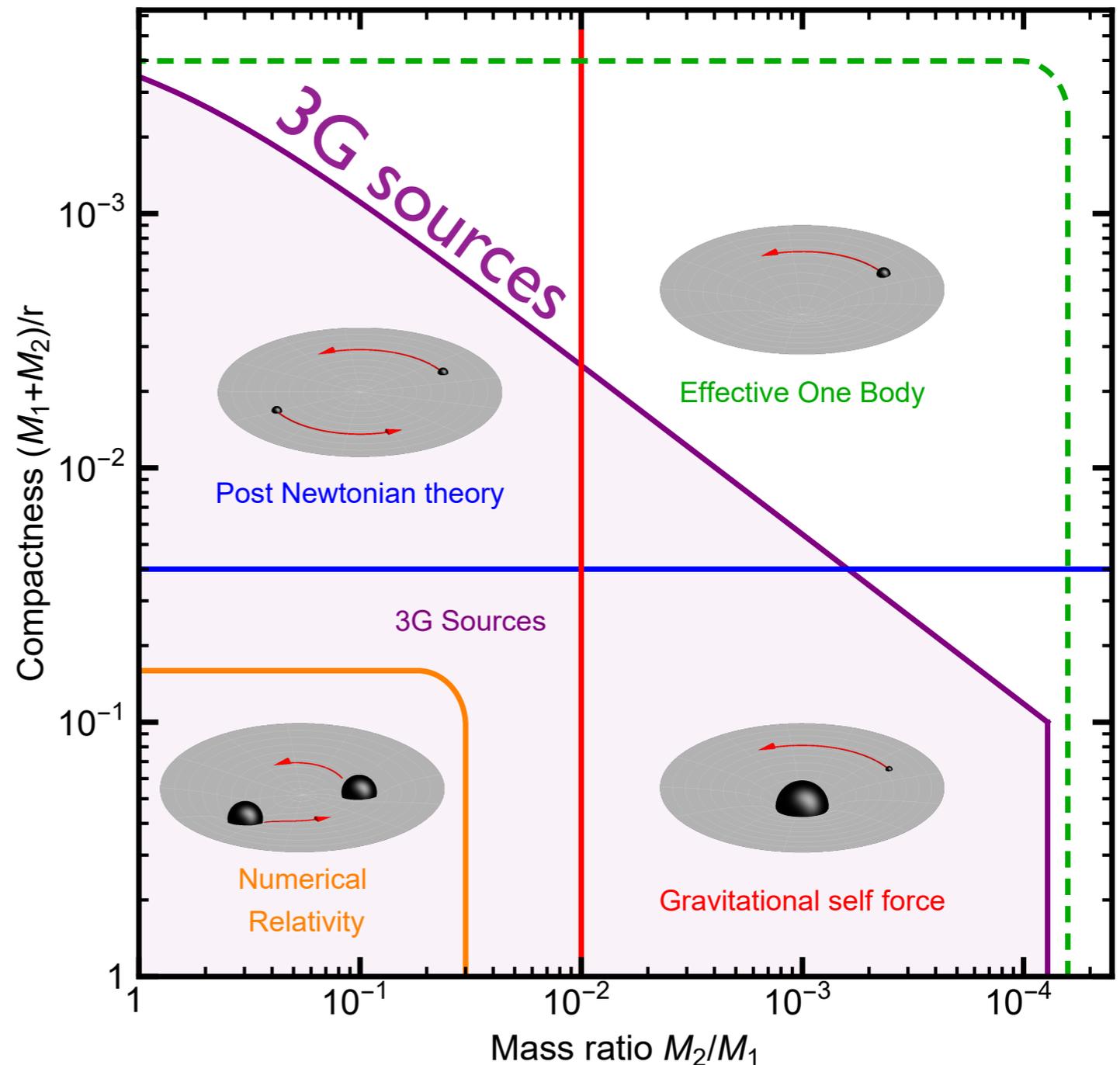


- 3G detectors will observe **binary coalescences with SNR** (~ 10) up to **redshift** ($z \sim 12$), and with **SNR** > 100 at $z < 2$.
- Demands on waveform **accuracy** are **higher**, modeling is more **challenging**.

Need to solve 2-body problem in larger region of parameter space with 3G

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R = \frac{8\pi G}{c^4}T_{\mu\nu}$$

- **GR** is **non-linear theory**.
- Einstein's field equations can be solved:
 - **approximately**, but **analytically** (**fast way**)
 - **“exactly”**, but **numerically** on supercomputers (**slow way**)



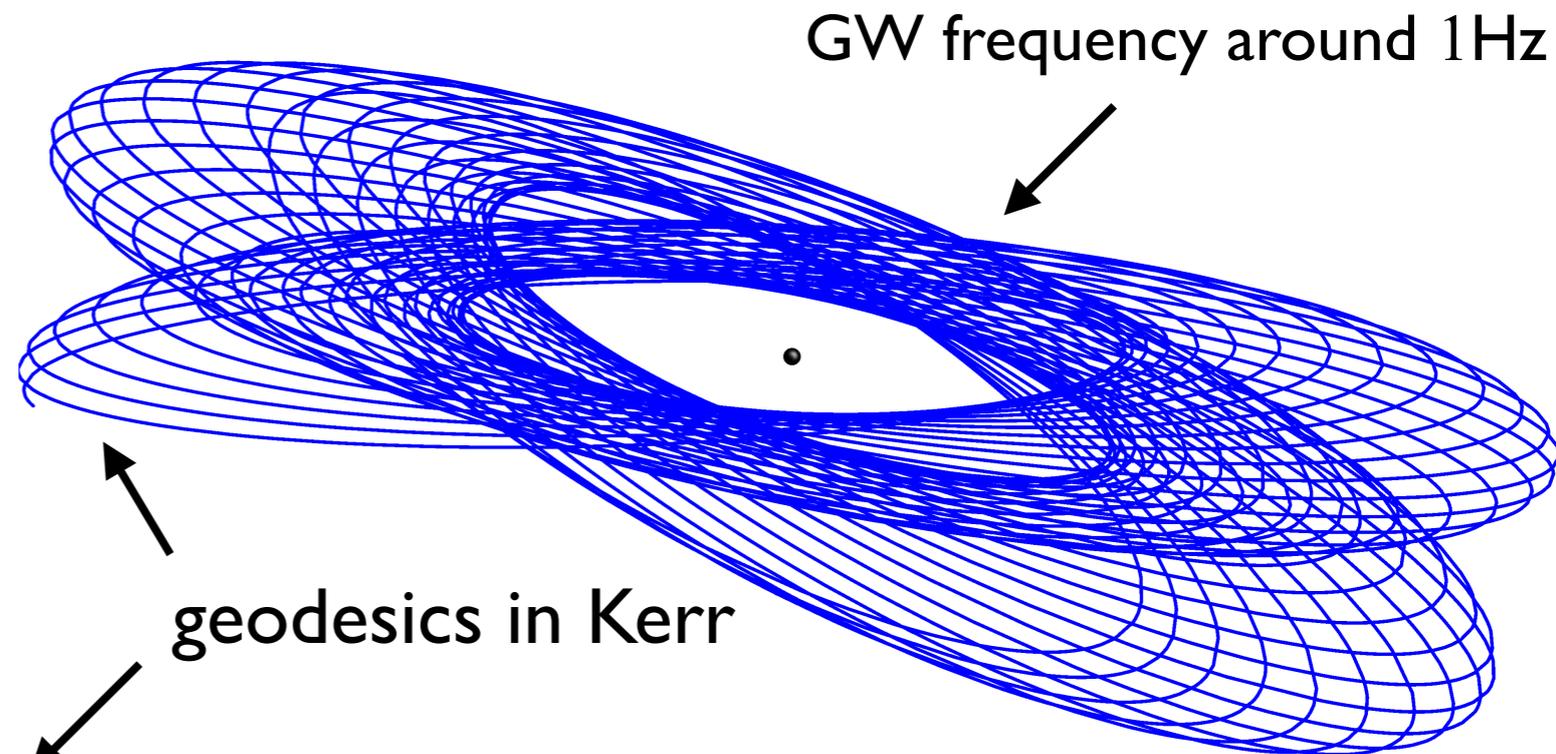
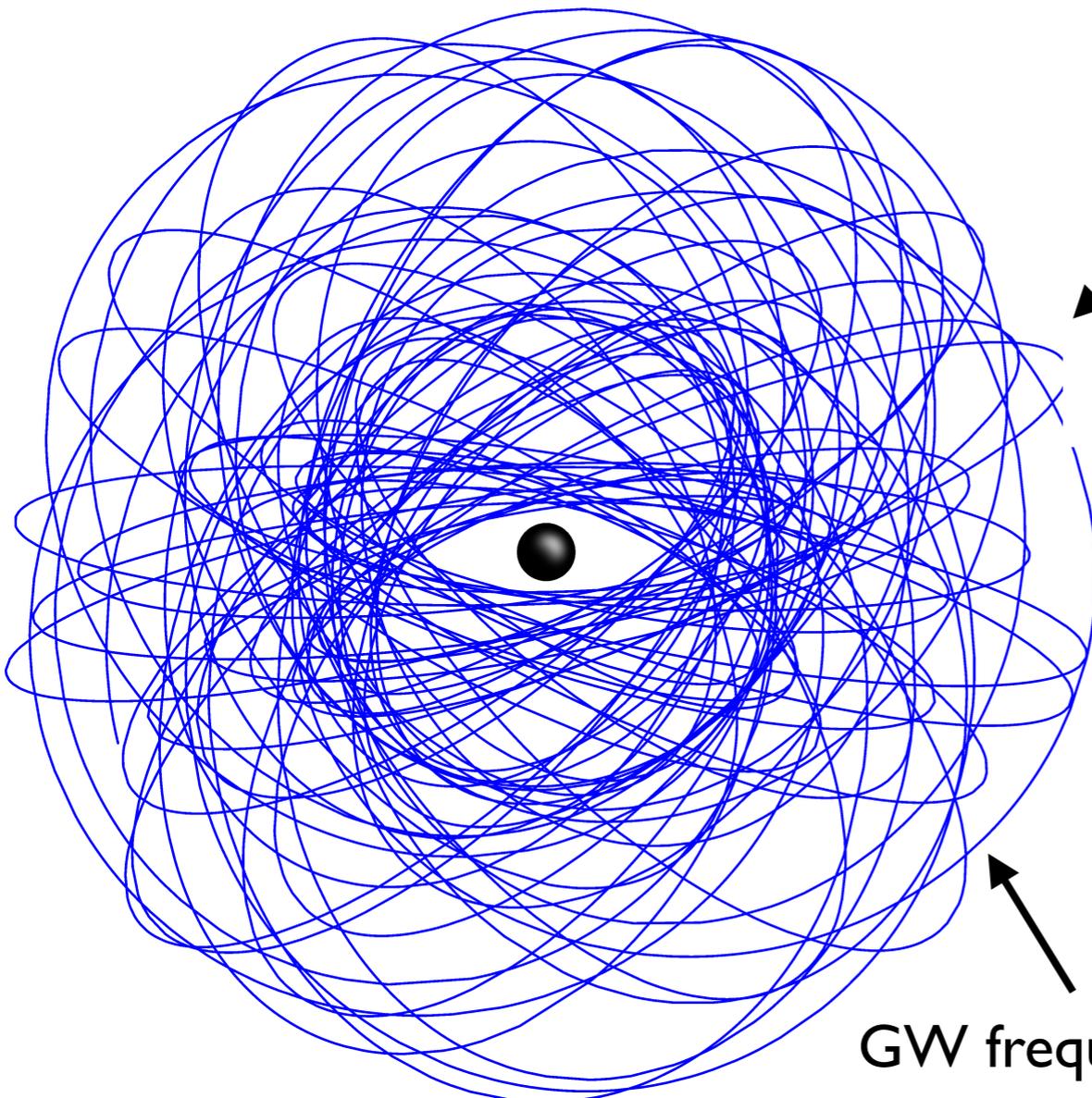
- **Synergy** between **analytical** and **numerical relativity** is **crucial**.

New sources with 3G detectors: intermediate-mass black-hole inspirals

- central BH's spin = 0.9

- eccentricity = 0.5

$$M = 1000M_{\odot}$$



geodesics in Kerr

- Sweeping in band for a **few thousand GW cycles**, probing **strong-field** gravity.
- **GSF** is likely to be important, we **need** to develop **accurate waveform models**.

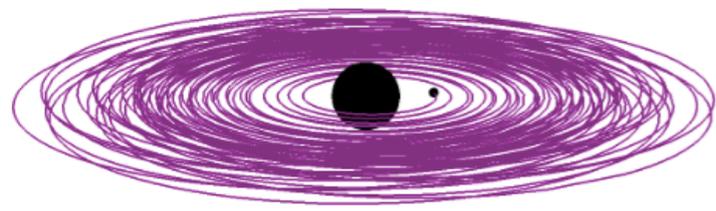
GW frequency around 10 Hz

3G science by including missing physical effects: eccentricity

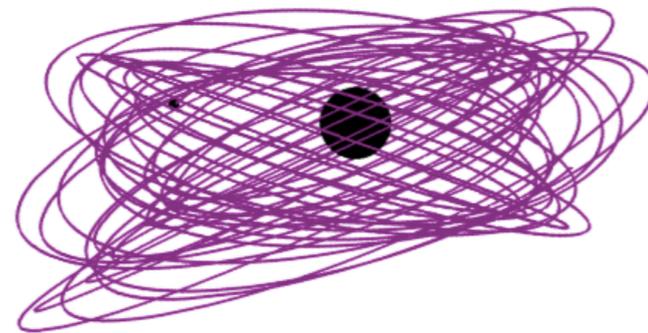
- How to **discriminate** among binary's **formation scenarios**, and **probe astrophysical environment**? **Eccentricity** and **spin-precession** can disclose this information.

- **Eccentric** compact-object **binary**:

NR simulation

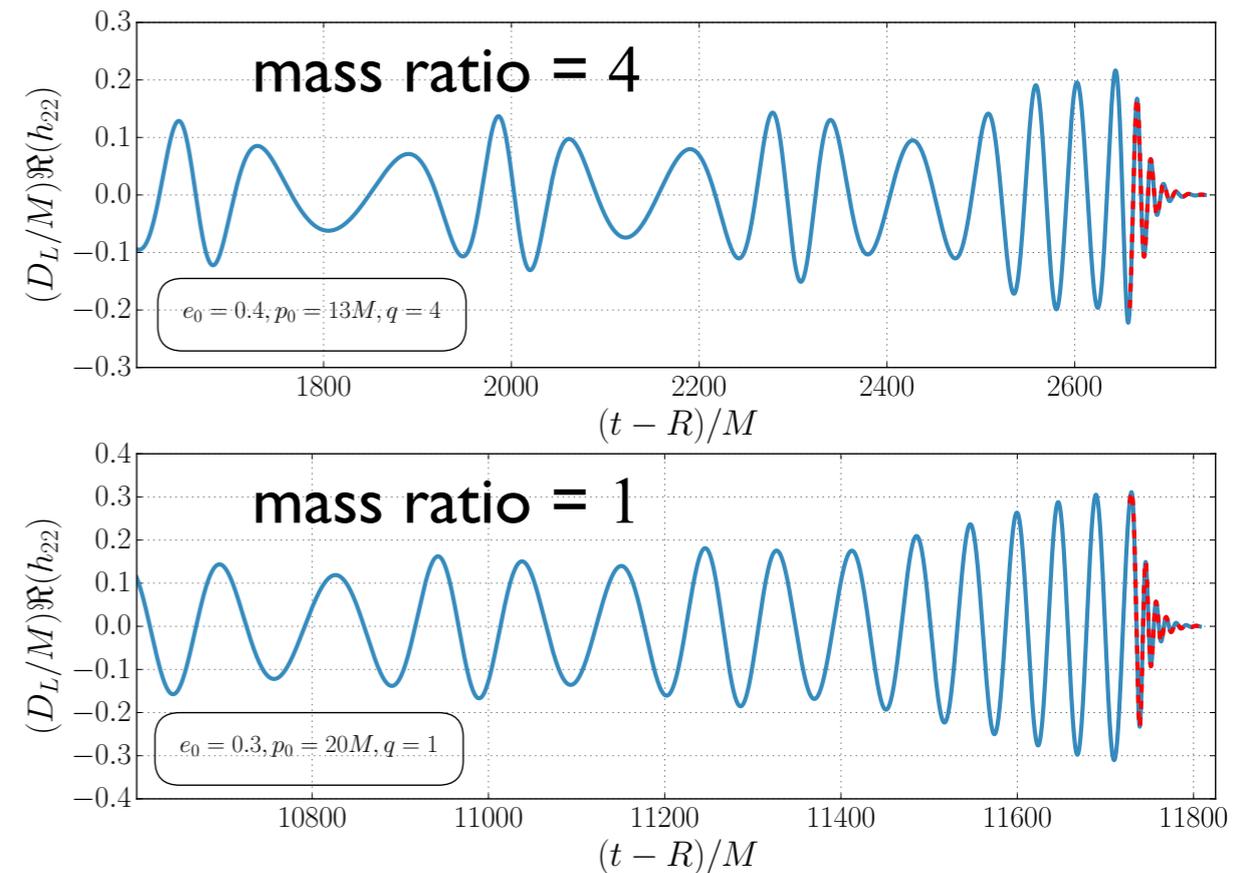


mass ratio = 7



(Lewis et al. 16)

AR waveform model

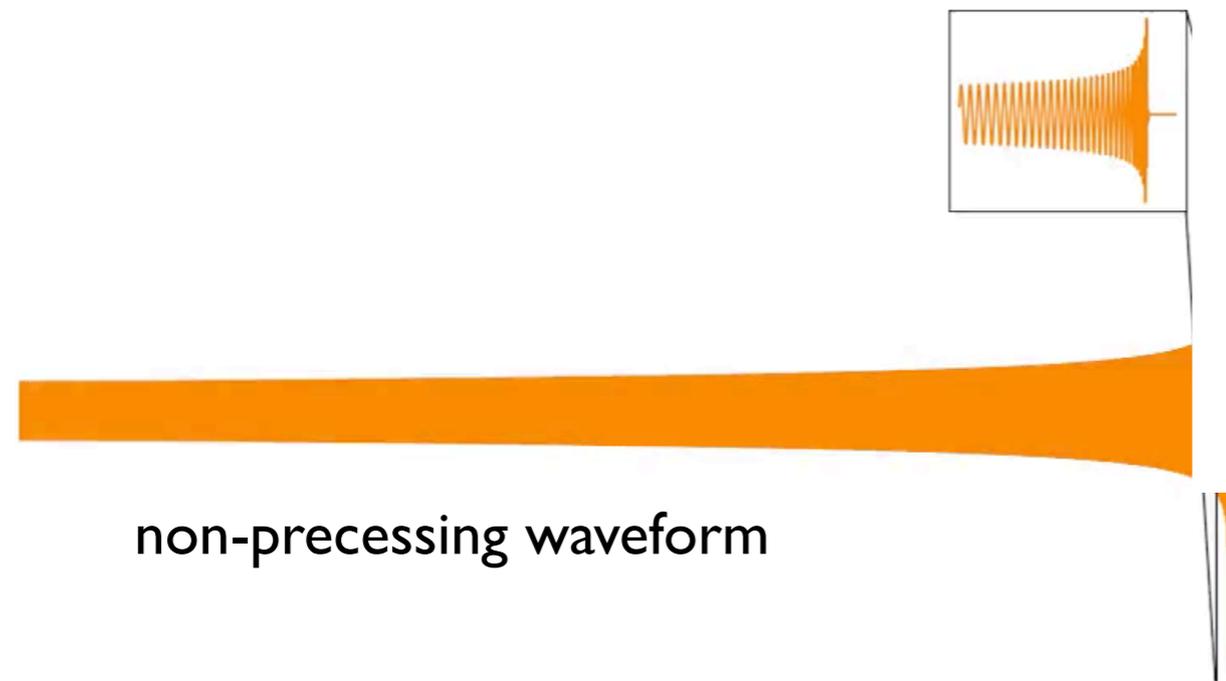
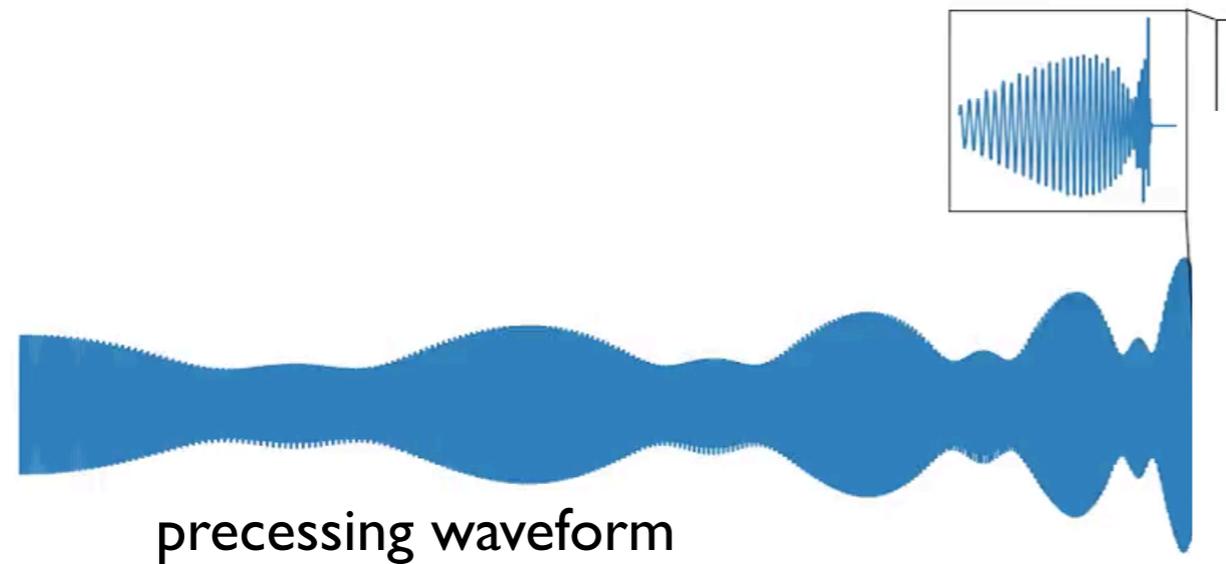


(Hinderer & Babak 17)

- We **need** accurate **waveform models** with **eccentricity** also for **stellar mass BBHs**.

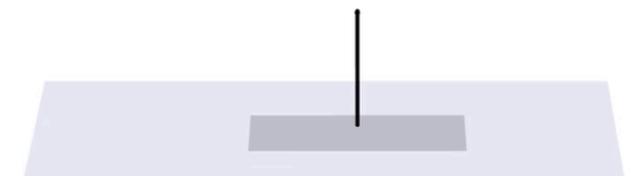
3G science by including missing physical effects: spin-precession

(credit: Ossokine)



total mass = $29M_{\odot}$
mass ratio = 5

574 GW cycles, from 10 Hz
5 precessional cycles
40 sec duration

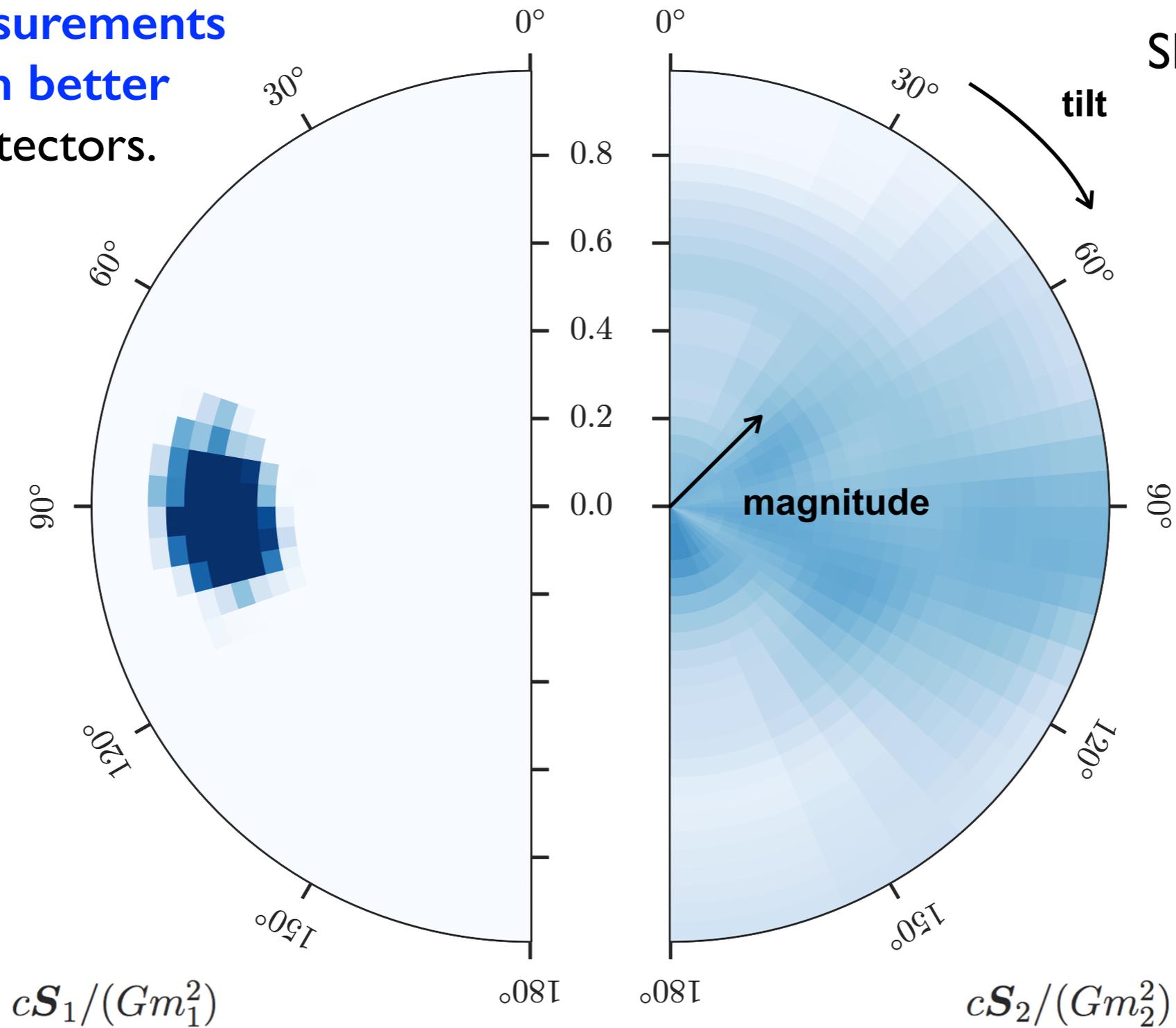


binary orbital plane

- **3G detectors** will observe **10^2 - 10^4 events** per year. We will observe **unusual events**.

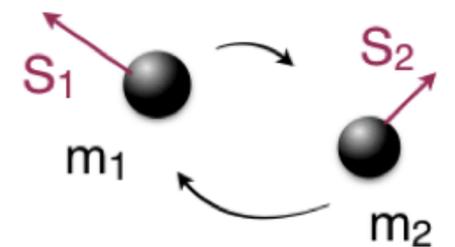
Measuring spin-precession with 2G detectors

- Spin measurements will be **even better** with **3G** detectors.



SNR = 25 with 2G

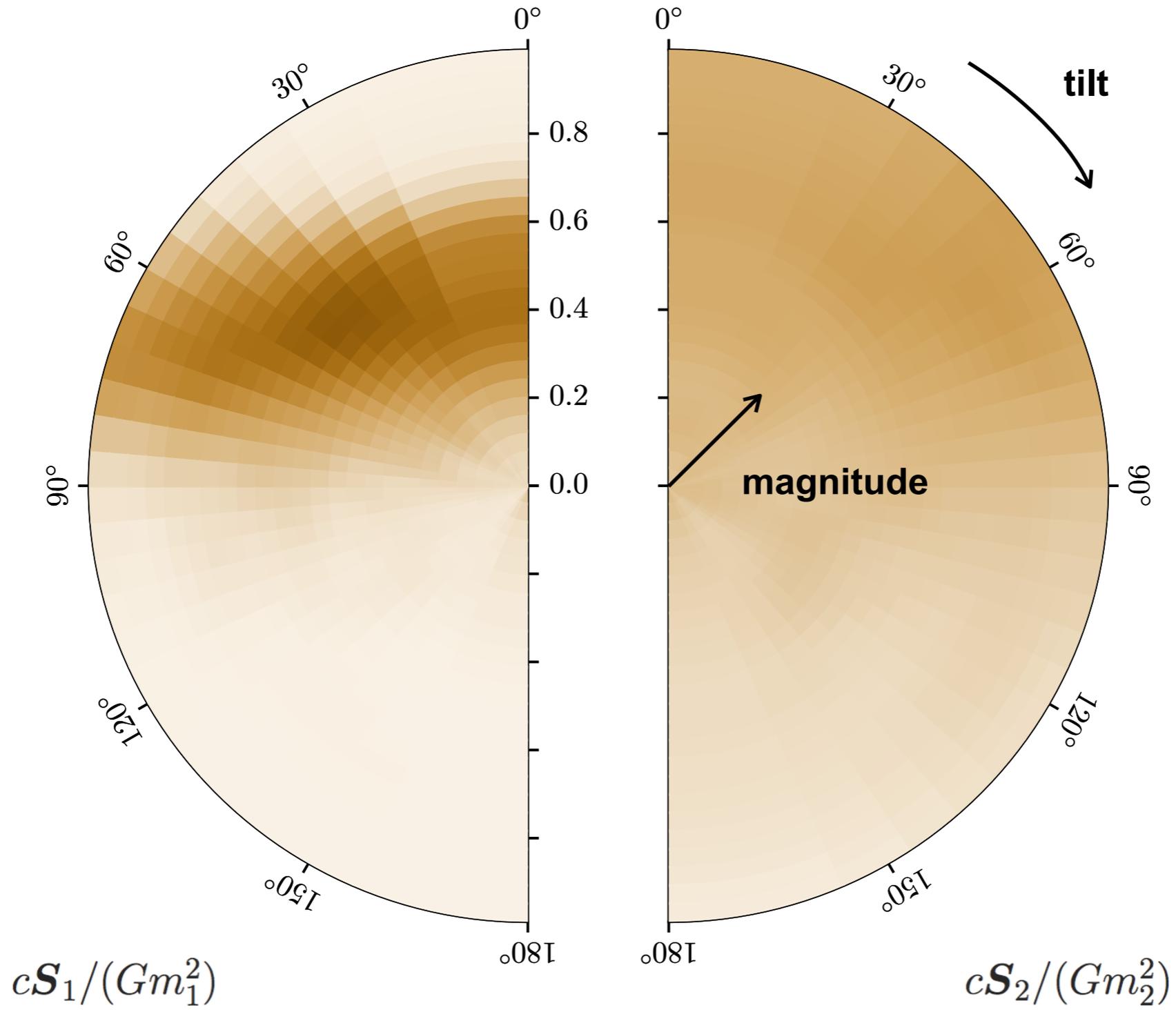
(credit: Pürrer)



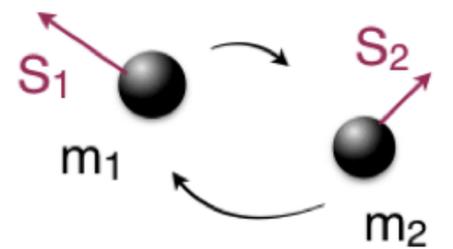
(credit: Hinderer)

Measuring spin-precession with GW151226

(Abbott et al. PRL 116 (2016) 241103)



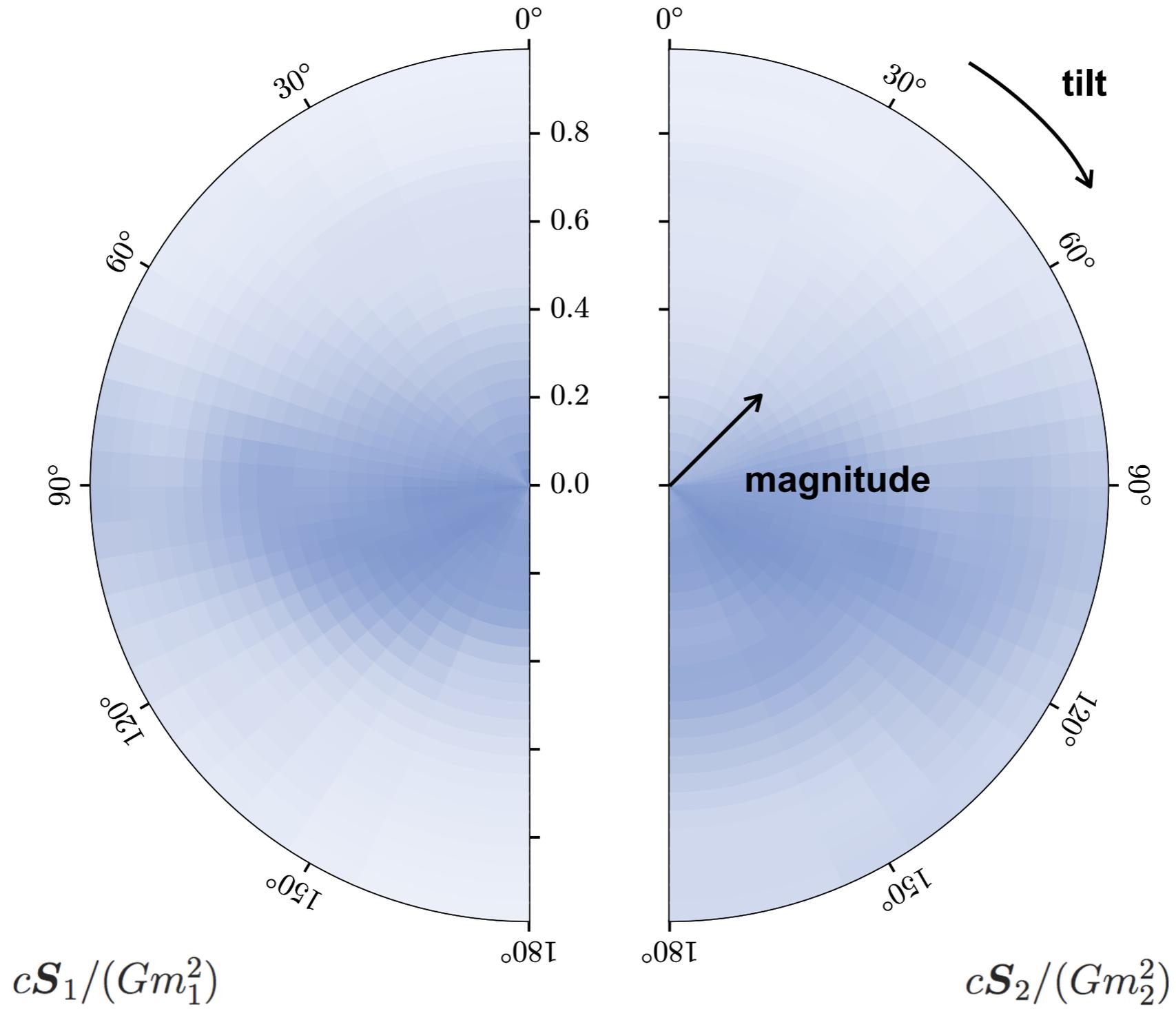
(credit: Pürrer/LIGO/Virgo)



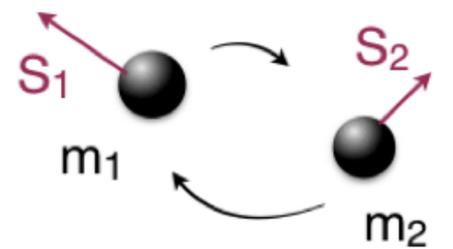
(credit: Hinderer)

Measuring spin-precession with GW150914

(Abbott et al. PRL 116 (2016) 061102)

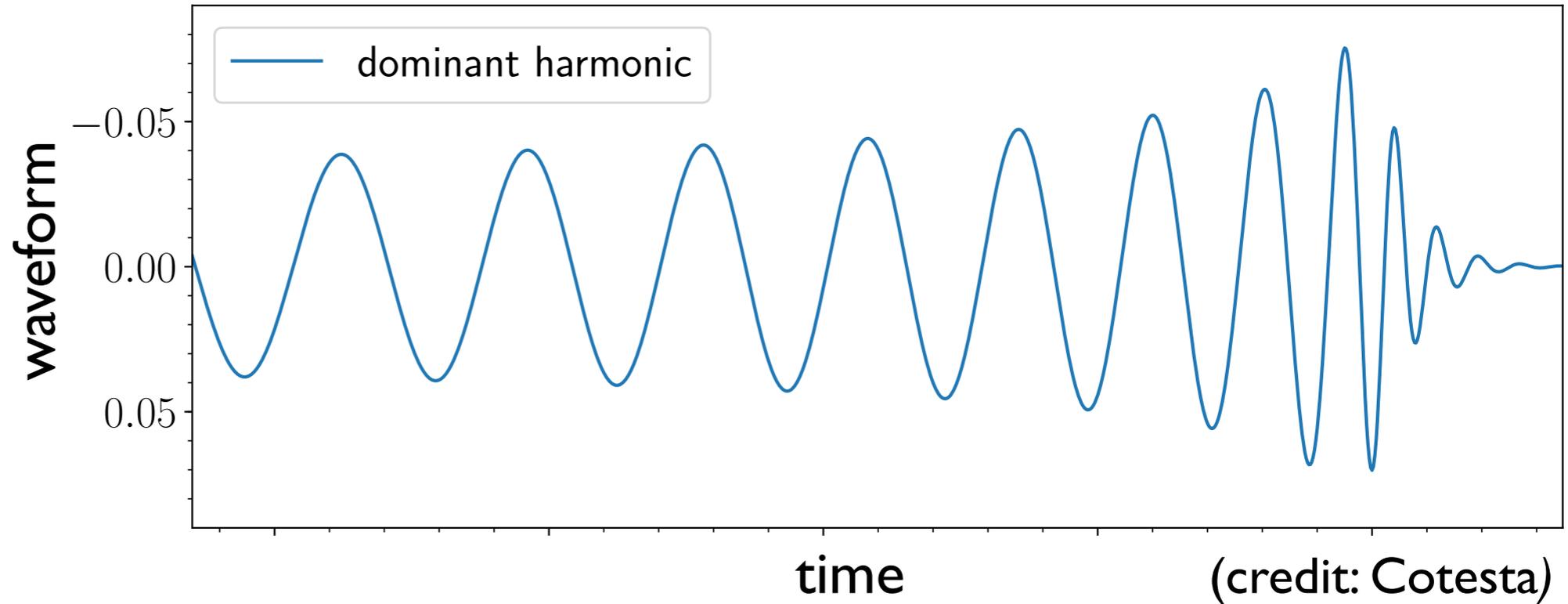


(credit: Pürrer/LIGO/Virgo)

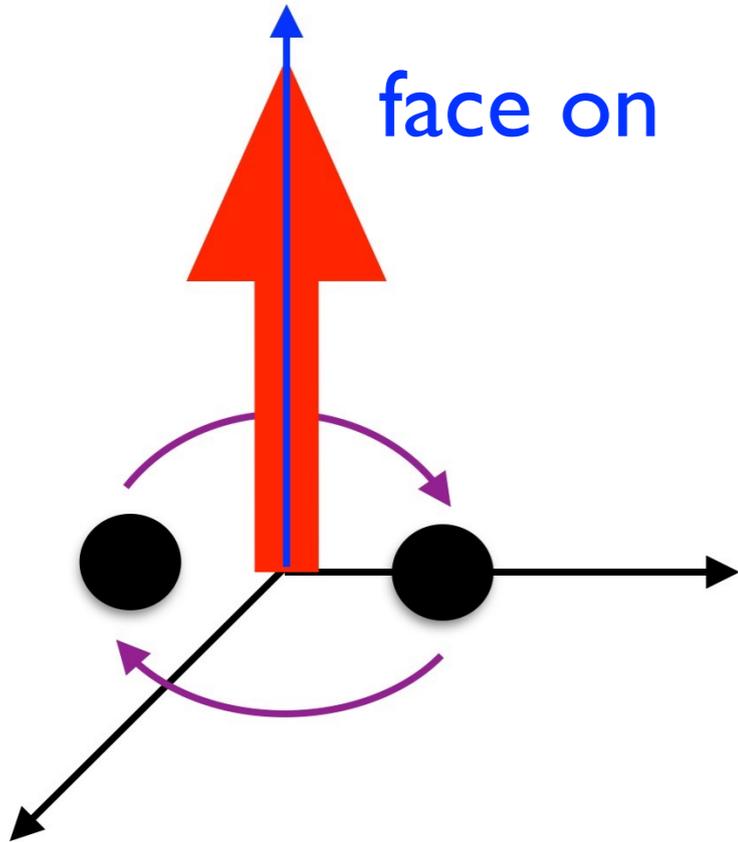


(credit: Hinderer)

3G science by including missing physical effects: higher harmonics



face on

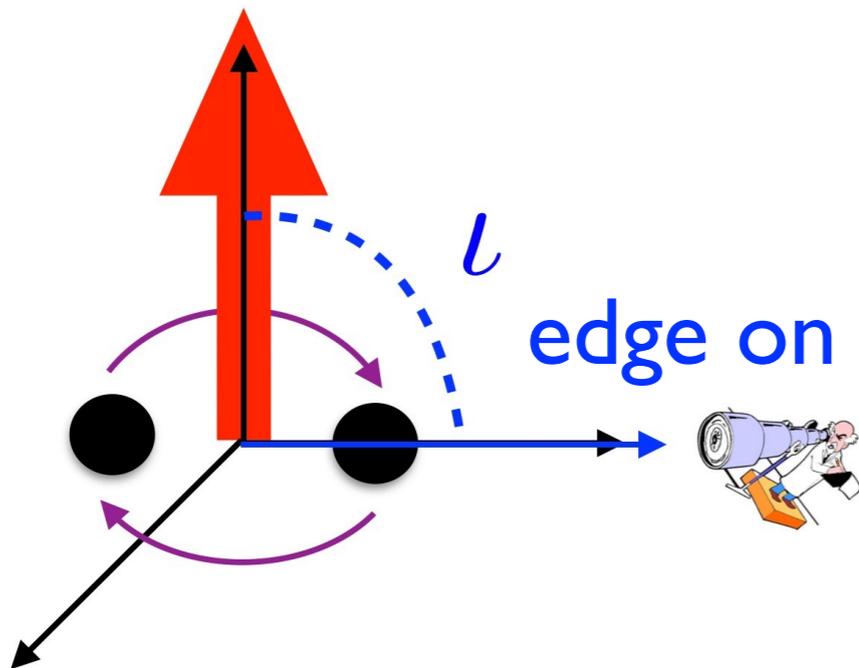
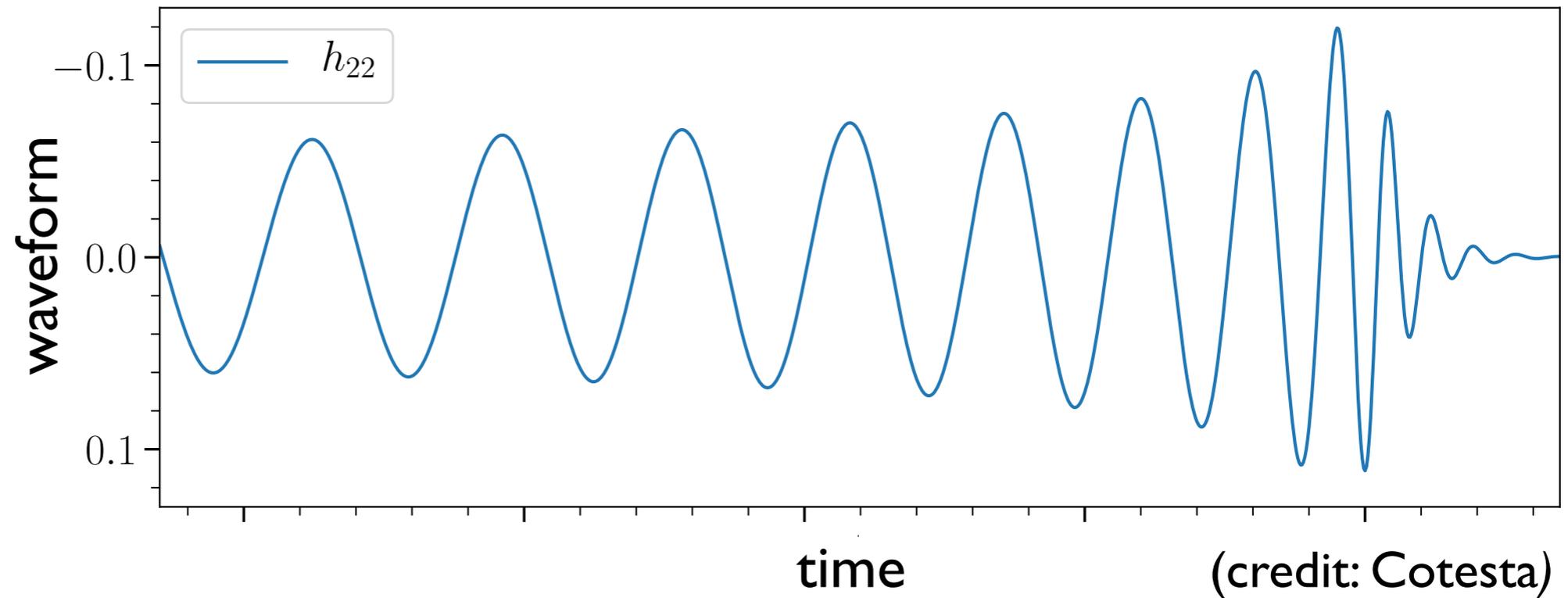


- So far, 2G detectors **observed GW events mostly face-on/face-off.**
- **Face-on/face-off orientation** suppress **higher harmonics, spin-precessional effects**, making **harder to infer** source's **properties.**

3G science by including missing physical effects: higher harmonics



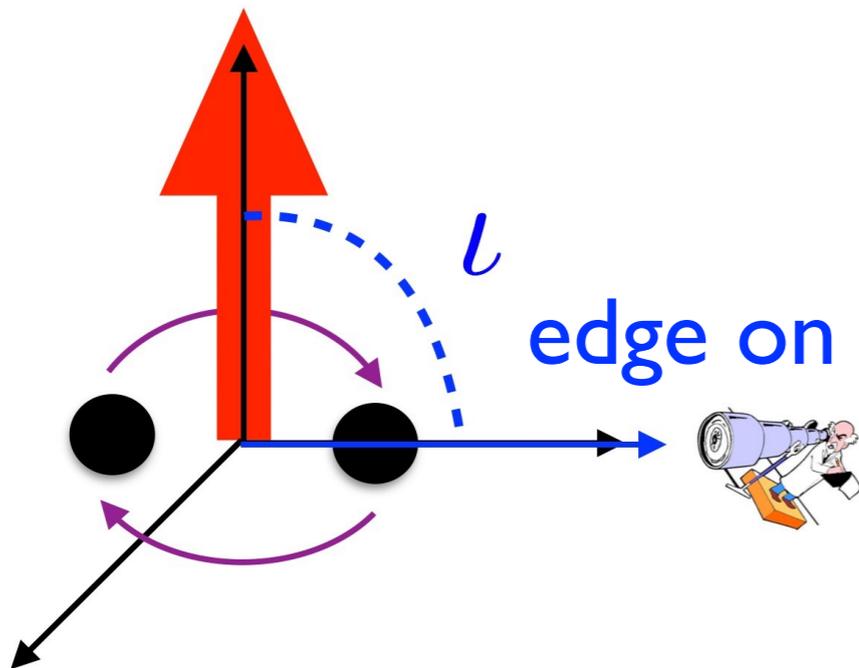
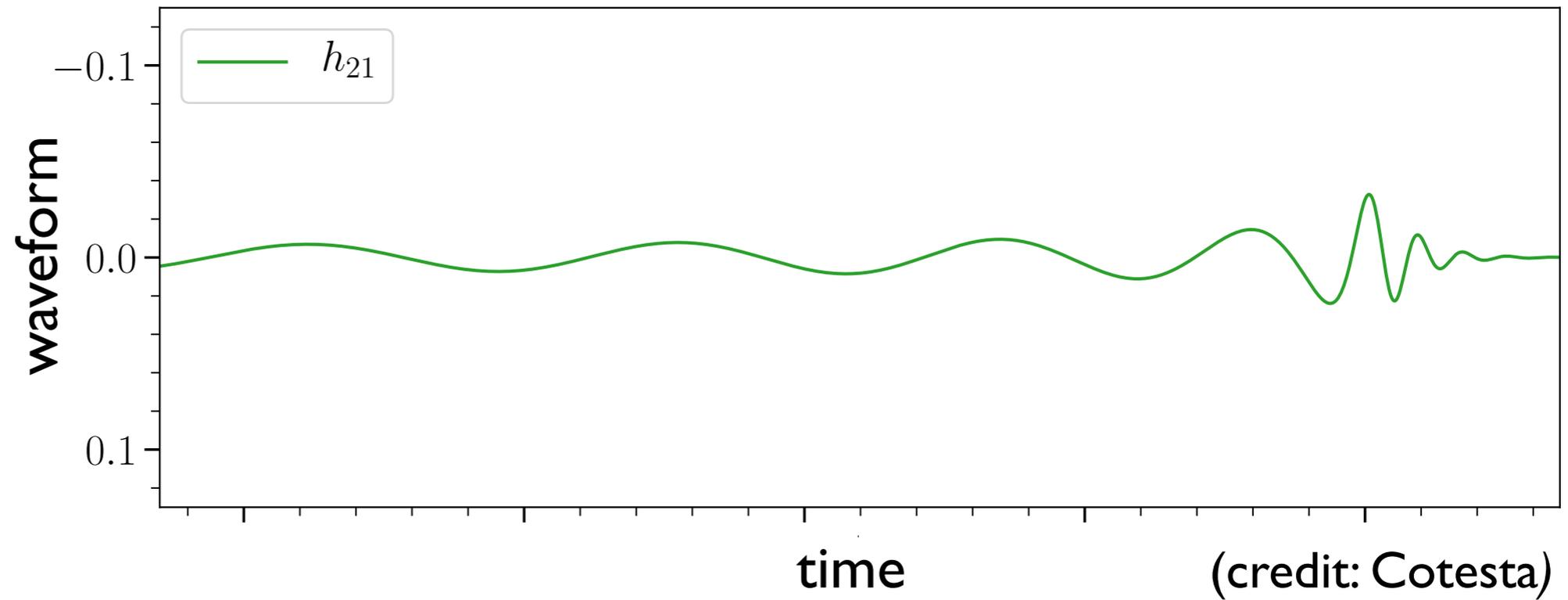
fundamental harmonic



3G science by including missing physical effects: higher harmonics



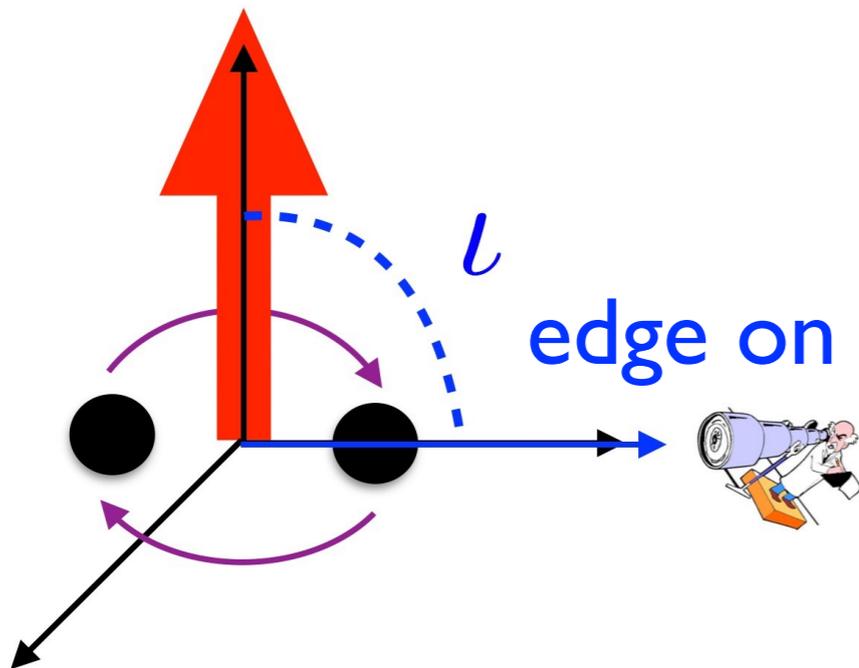
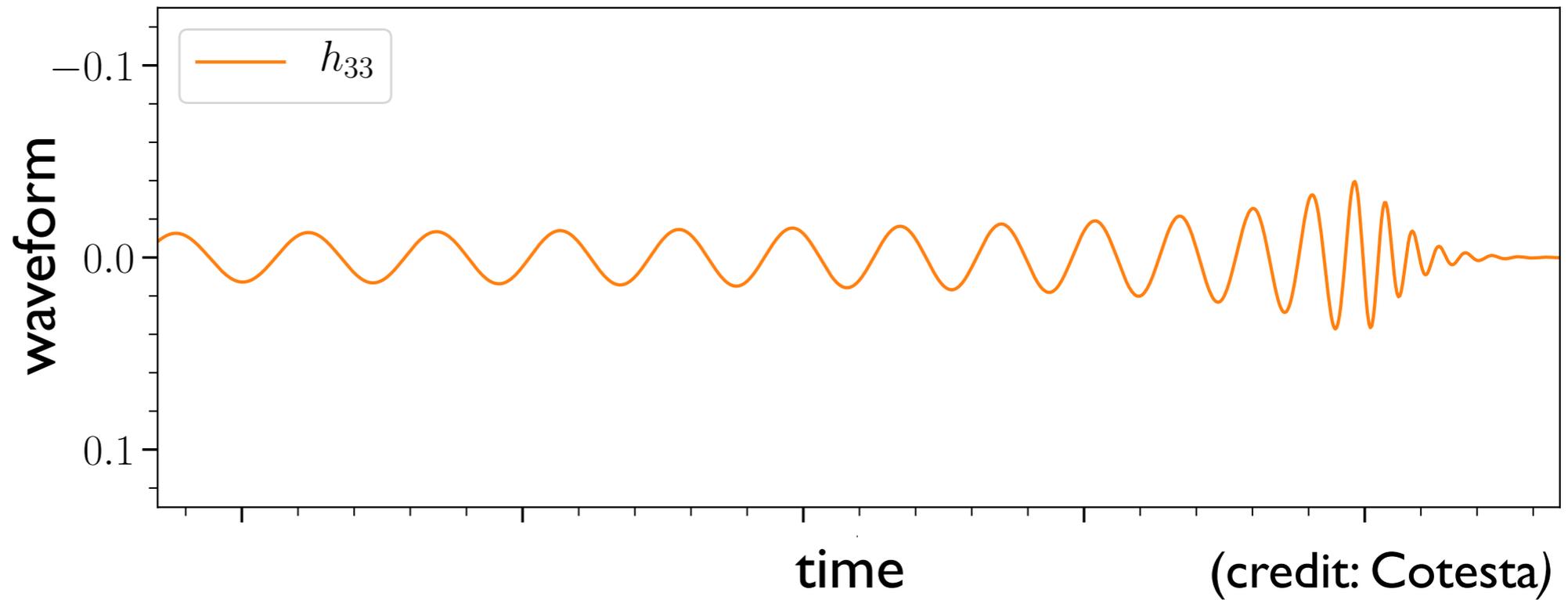
first harmonic



3G science by including missing physical effects: higher harmonics



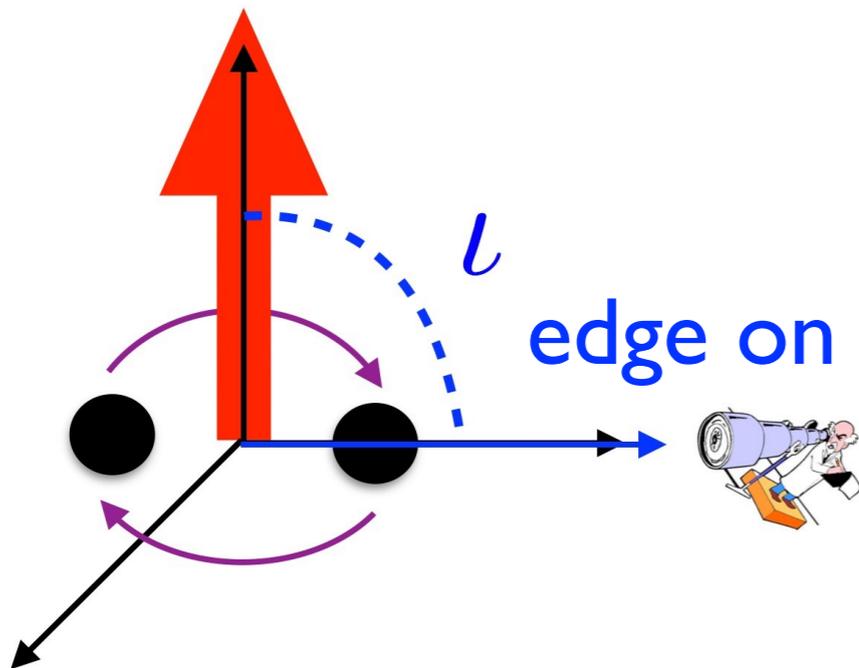
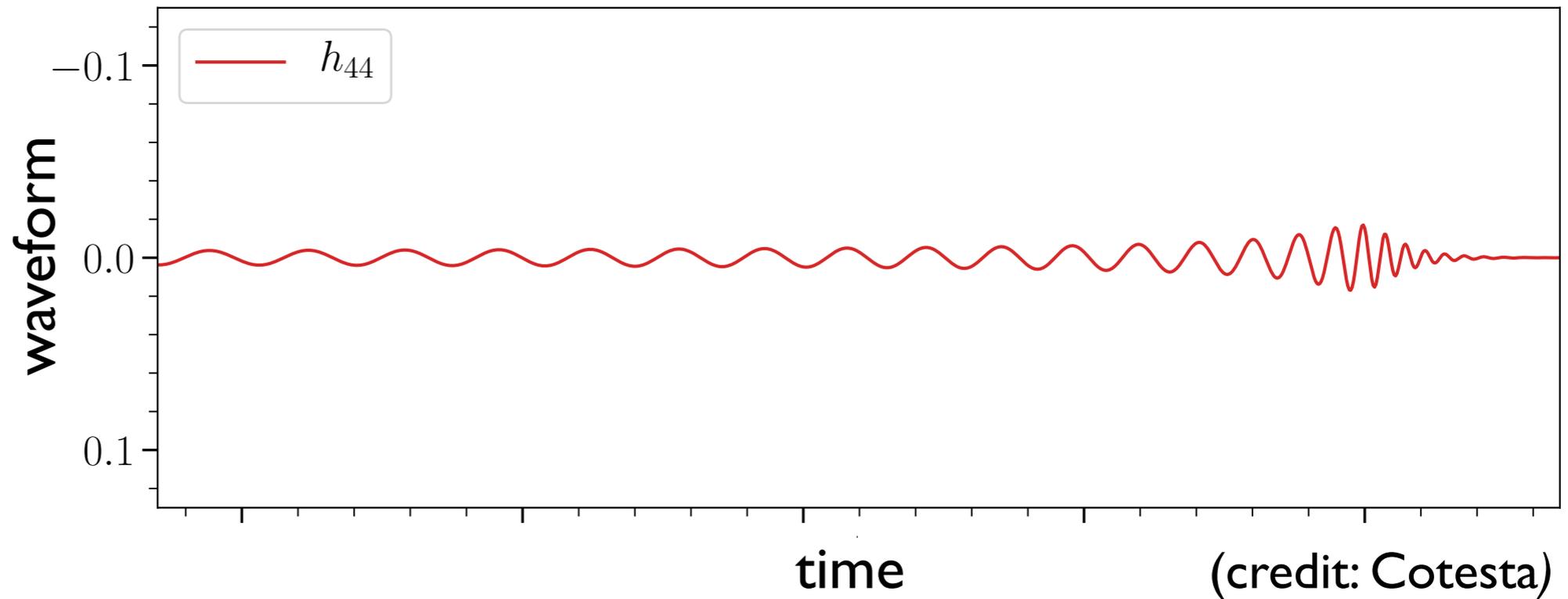
third harmonic



3G science by including missing physical effects: higher harmonics



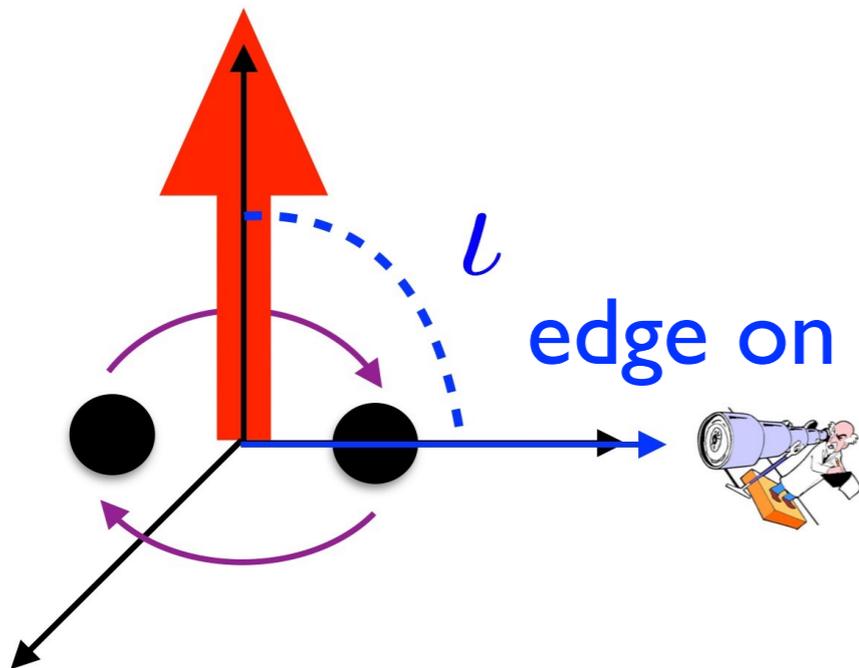
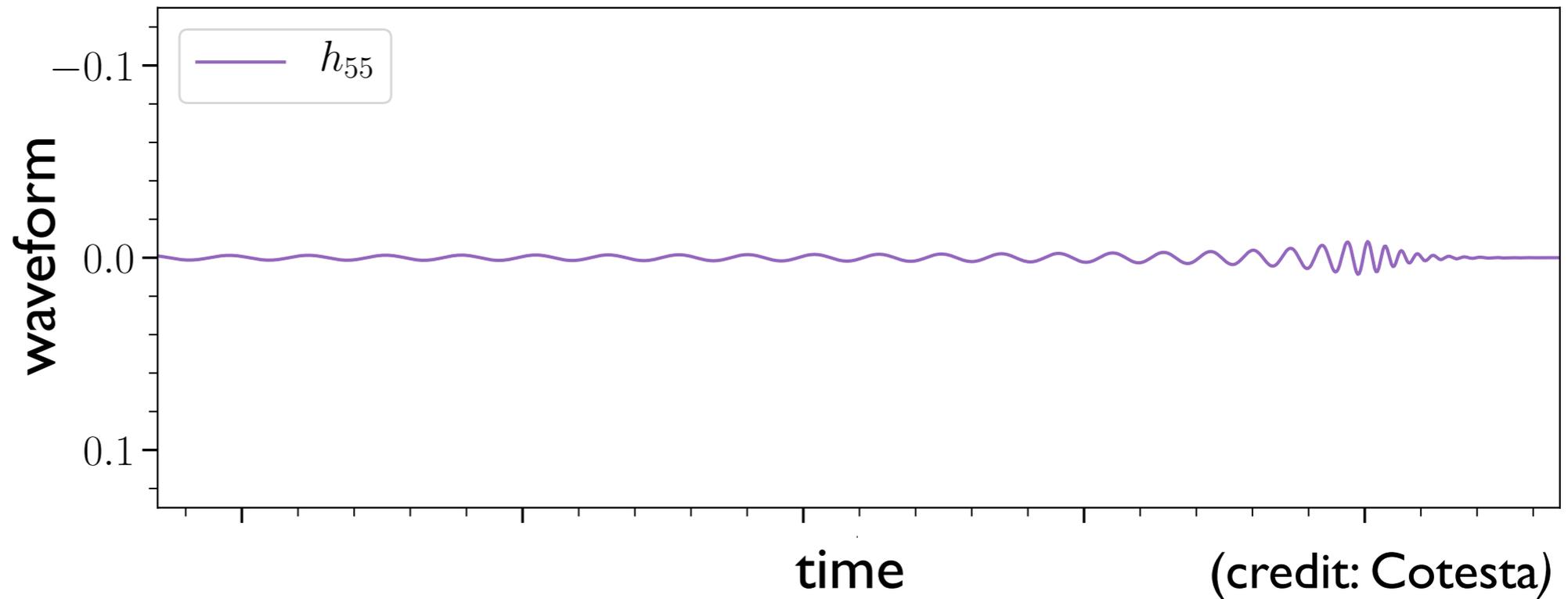
fourth harmonic



3G science by including missing physical effects: higher harmonics

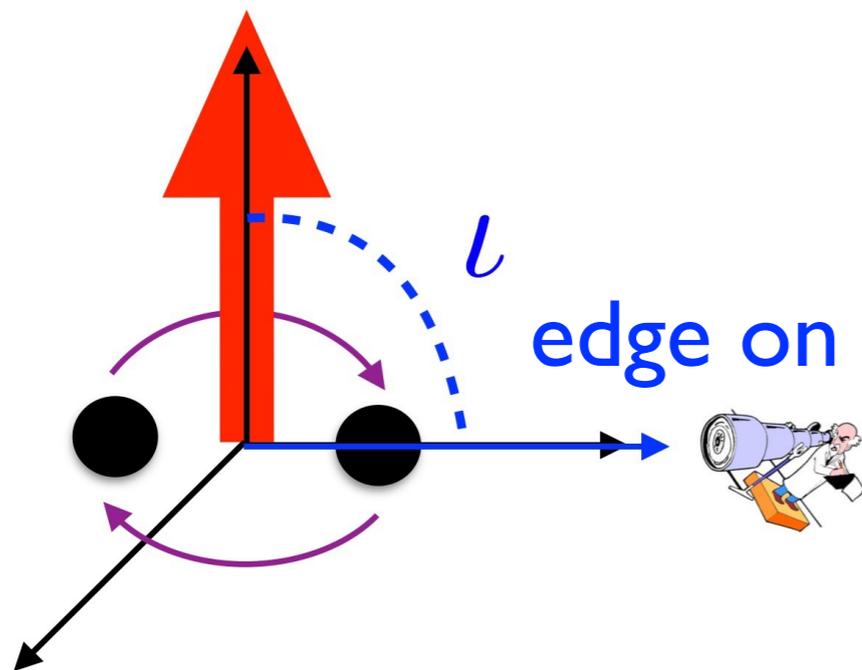
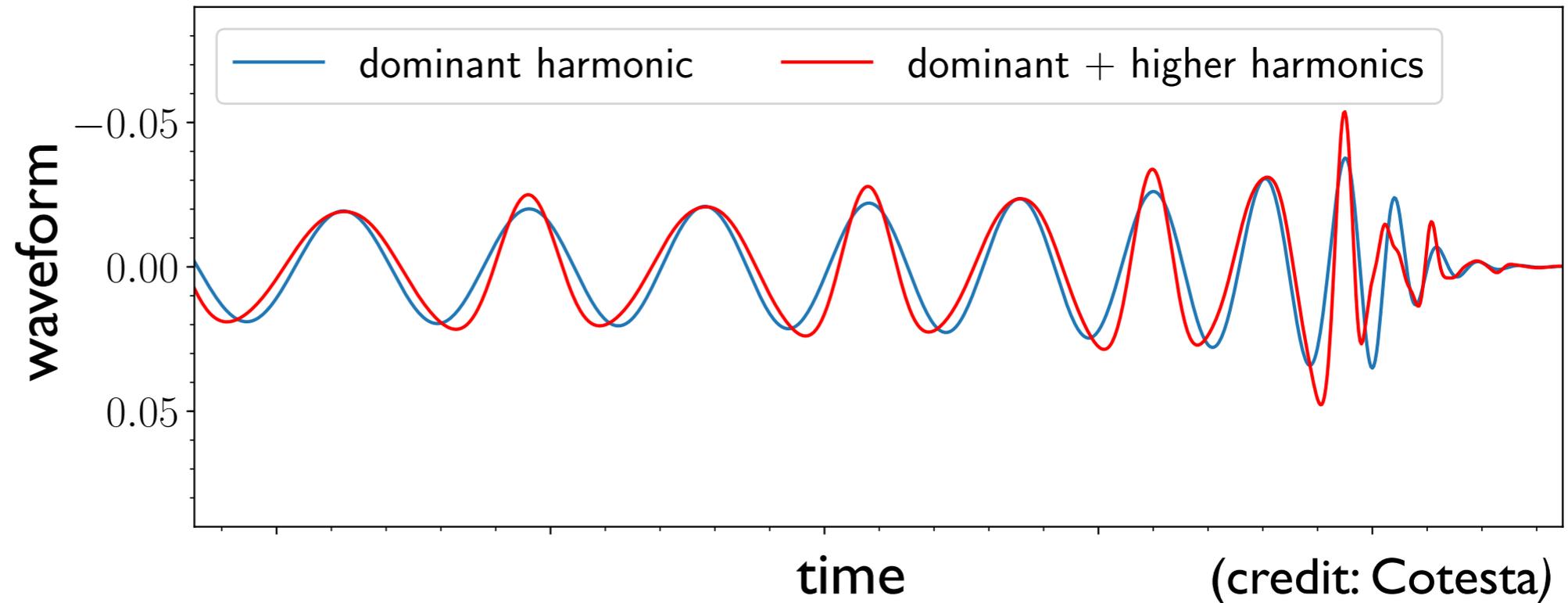


fifth harmonic



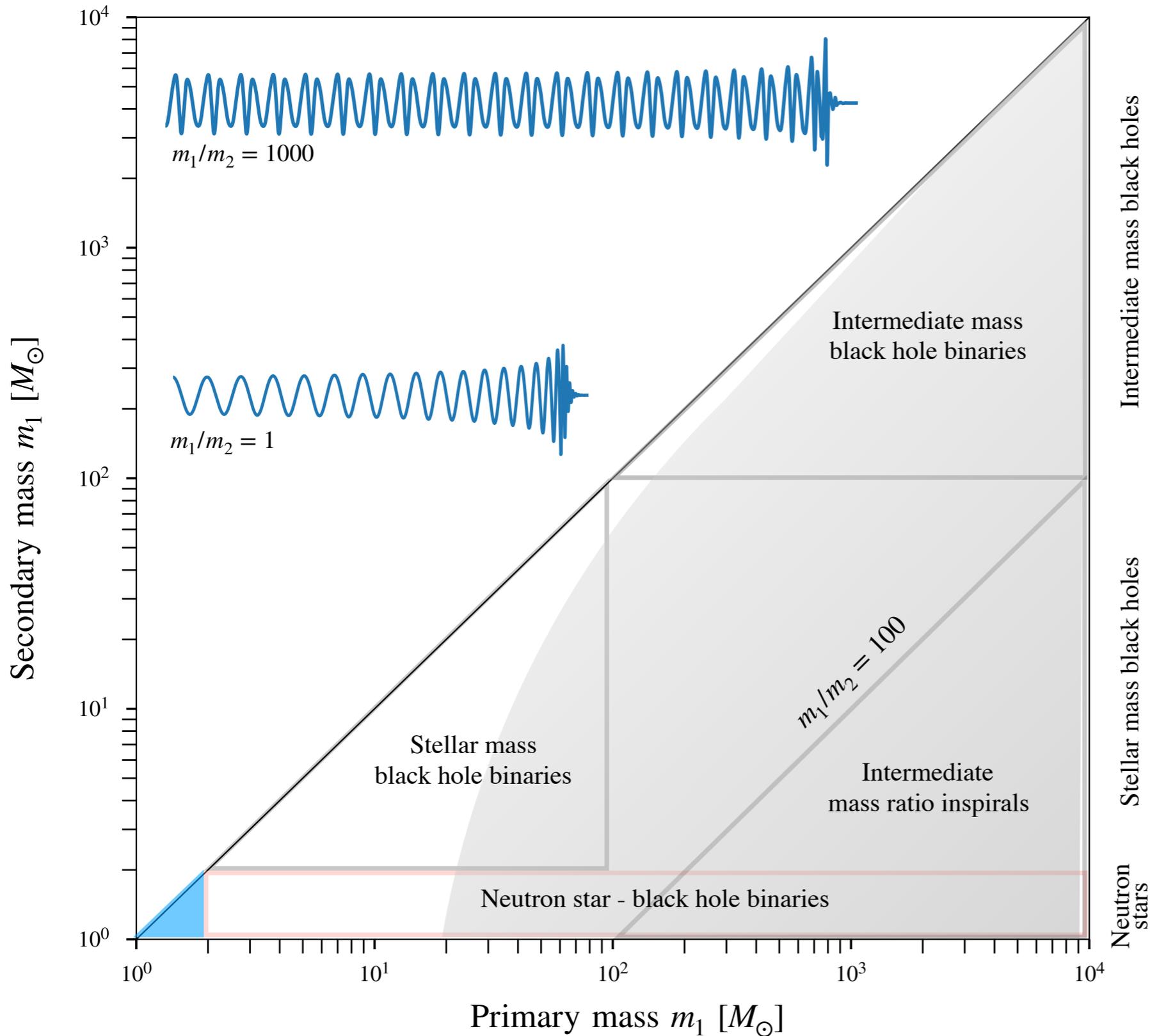
3G science by including missing physical effects: higher harmonics

adding all five harmonics



- We will **detect unusual** GW events with 3G detectors.
- We need accurate waveform models with **higher harmonics, spin precession & eccentricity.**

Relevance of higher harmonics for 3G detectors

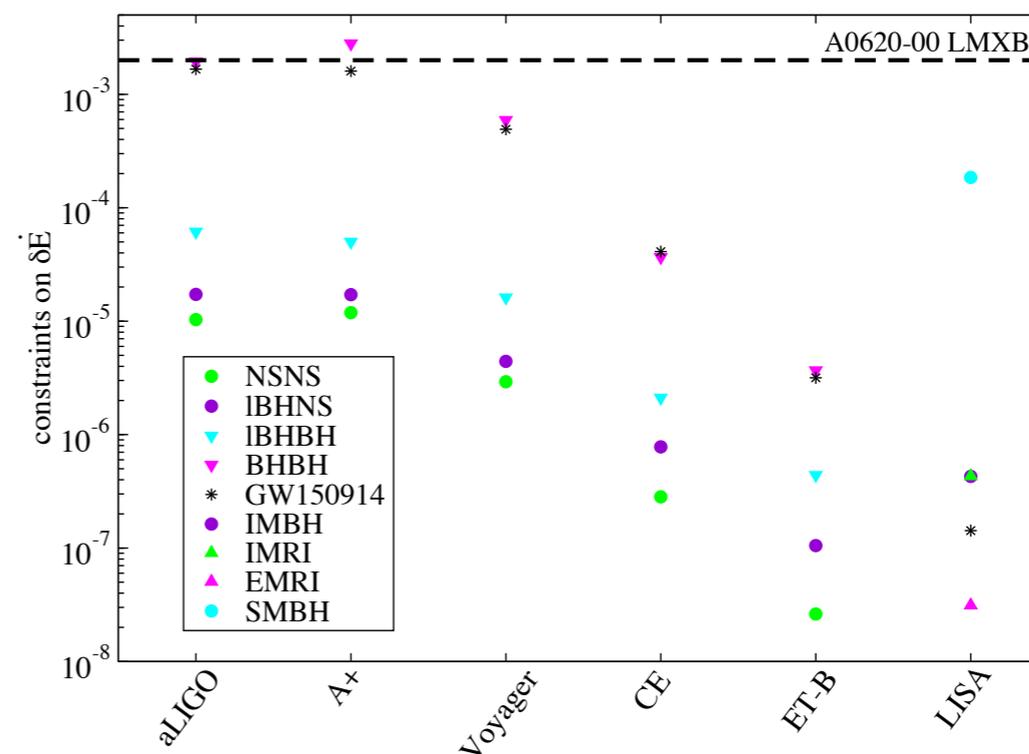
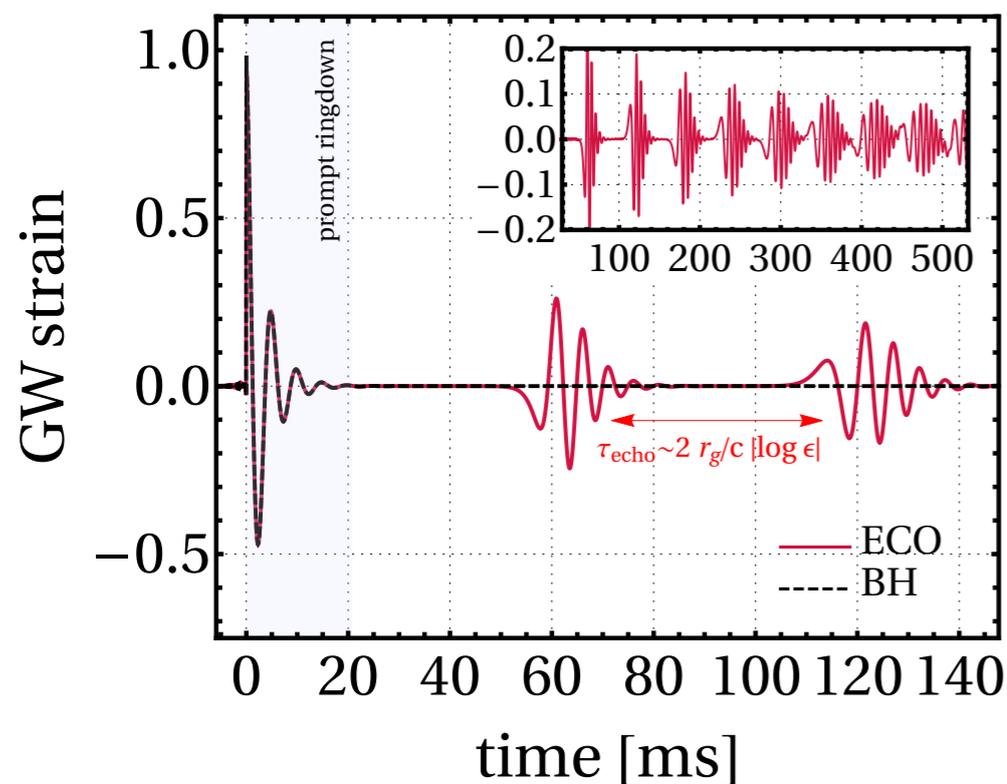


Gray region: more than **10% loss** in detection rate, thus **impacting parameters inference** and **science**.

2G placeholder to be replaced by 3G results.

Need waveforms to test GR and probe nature of compact objects

- Need **AR & NR waveforms** in **modified theories of GR**: scalar-tensor theories, Einstein-Aether theory, dynamical Chern-Simons, Einstein-dilaton Gauss-Bonnet theory, massive gravity theories, etc.
- Need **AR & NR waveforms** of binaries composed of **exotic compact objects** (BH & NS mimickers), such as boson stars, gravastar, etc.
- Can we **disprove** the **presence** of BH “**horizon**” in binary mergers? **QNMs not consistent** with GR. **Echoes. Need modeling.**



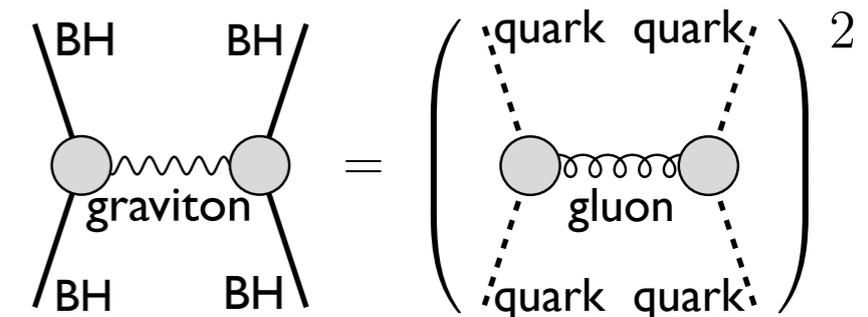
Need novel and efficient methods to solve 2-body problem

- Finite difference/spectral NR codes cannot be simply adapted to achieve **higher accuracy** over **longer evolutions** of compact objects with **large spins** and **mass ratios**. **Novel algorithms** are needed for **3G** detectors.
- Genuine **computations of PN/PM/GSF** corrections at **higher order** are **needed** but **will not solve accuracy** problem by themselves.

(credit: Justin Vines)

		0PN	1PN	2PN	3PN	4PN	5PN	...
0PM:	1	v^2	v^4	v^6	v^8	v^{10}	v^{12}	
1PM:		$1/r$	v^2/r	v^4/r	v^6/r	v^8/r	v^{10}/r	
2PM:‡			$1/r^2$	v^2/r^2	v^4/r^2	$v^6/r^2‡$	$v^8/r^2‡$	
3PM:				$1/r^3$	v^2/r^3	v^4/r^3	v^6/r^3	
4PM:					$1/r^4$	v^2/r^4	v^4/r^4	
...					

- **Modern scattering amplitude** methods of particles **applied to 2-body problem in GR?**



- **EOB** may combine efficiently PN/PM/GSF & NR, but it is likely that it **would need to be enhanced, tested and improved for 3G era**.
- **3G detectors** offer a challenging but exciting **opportunity** to build new **methods** (universal method?) to **solve 2-body problem** in entire parameter space.

Question

Is there **anything else** we should be **high-lighting** in the report about **challenges in waveform modeling** that would need to be addressed and solved to achieve **3G-detector science**?