The Landscape of String Vacua

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- The Planck satellite will be launched to measure the anisotropies in CMB with new precision → descriminate among various inflationary scenarios





 The Glast (Gamma-ray Large Area Space Telescope) will be launched into orbit to take a gamma-ray image of the sky → dark matter



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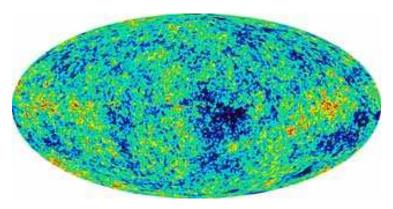
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- Unification of QFTs and gravity





Experimental evidence for a Big Bang scenario with an inflationary epoch

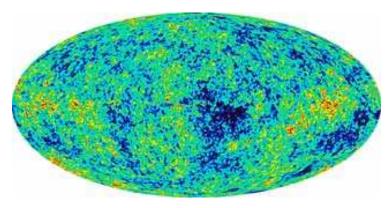


WMAP: CMB anisotropies

Cosmology

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• The observable universe is flat with $\Omega_M = 0.3$ and $\Omega_\Lambda = 0.7 \rightarrow \text{dark matter}$ and dark energy

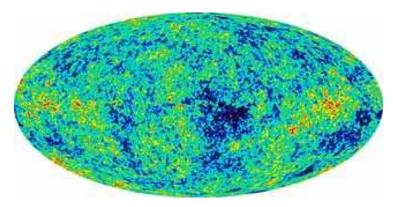


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- existence of extremal objects in the universe as for instance Black Holes



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The solutions of these problems seem to lie beyond the established theories of the Standard Model and General Relativity.

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- Extension of SM with little Higgs, etc.

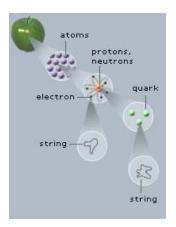
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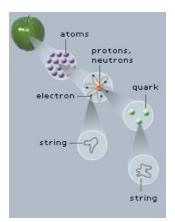
String Theory is a candidate solution to more ambitious theoretical questions like

- Ultraviolet finite quantisation of gravity, space-time at very short distances
- Statistical interpretation of black hole entropy
- Unification of gauge theories and gravity in one theoretical framework

Fundamental objects: Strings of length $\ell_s = 1/M_s$ (fundamental length scale) + D-branes

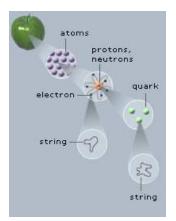


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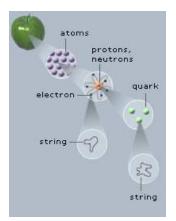


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Massless strings excitation: $G_{\mu\nu}$, ϕ , C_p

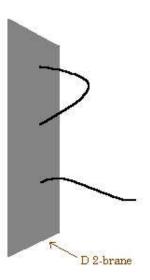
Massless strings excitation: $G_{\mu\nu}$, ϕ , C_p These p-forms C_p couple to a p-dimensional object, so-called (p-1)-branes.

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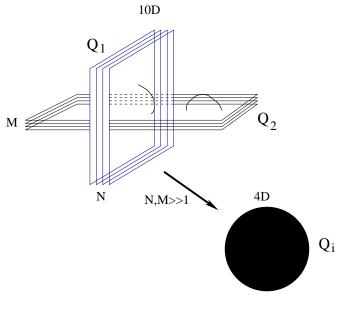
non-perturbative, solitonic objects, fluctuations \rightarrow open strings



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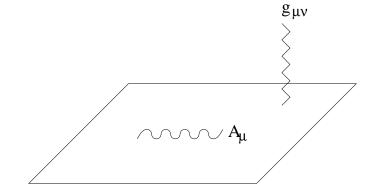
entropy of black holes: S = A/4



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gauge fields propagate on D-branes: U(N), SO(2N), SP(2N)



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- Is there any relation to other approaches of quantum gravity?

Fundamental problems of "applied" string theory (string phenomenology):

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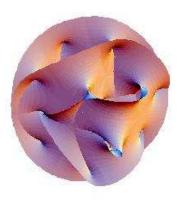
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- Does there exist (a so far unknown) dynamical process which (uniquely) selects this vacuum? (vacuum selection principle)

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Scenario I:

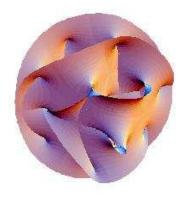
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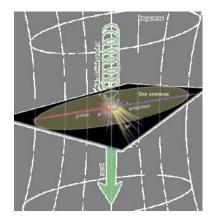
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Scenario II:

The gauge interactions are confined on 4D hypersurface (Brane) in 10D. Only gravity in 10D.



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Supersymmetry breaking: Dynamical supersymmetry breaking on hidden E_8^H mediated gravitationally to observable E_8 .

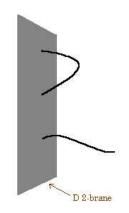
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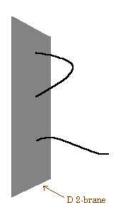
Details of MSSM physics depend on geometry of (X, V), i.e. the details of moduli stabilisation and the details of susy breaking + generated soft susy breaking terms.

Also $g_s = \exp(\phi)$ is a modulus.

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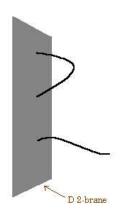


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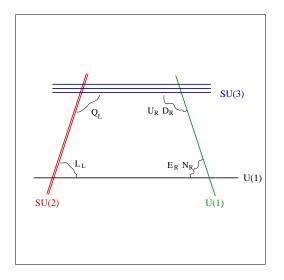
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so that with $g_s < 1$ one gets $M_{pl}^2 = M_s^{8-p}V_t$, $(V_X = V_t V_p)$. A small M_s can be traded for a large transversal dimension V_t ! Three cases: $M_s = 1$ TeV, $M_s = 10^{11}$ GeV, $M_s = 10^{17}$ GeV.

 $M_s = 10^{17}~{\rm GeV}:$ Susy at string scale + susy breaking by fluxes or dynamically

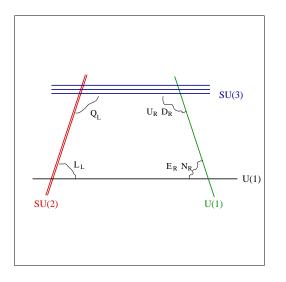
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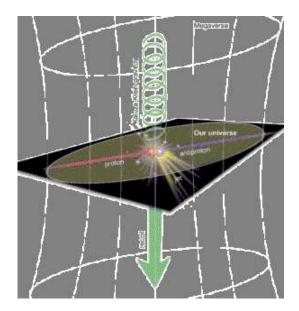


Possible string compactifications, mechanisms for moduli stabilisation and the determination of the 4D effective action for the light $m < M_s$ modes are under investigation (string phenomenology).

 $M_s = 1$ TeV: no susy at M_s necessary + large extra dimensions

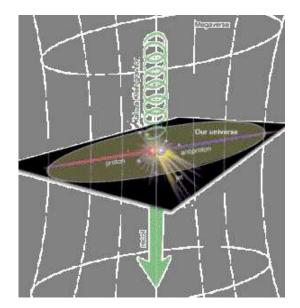
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String or KK modes at TeV scale



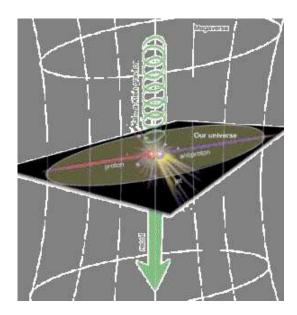
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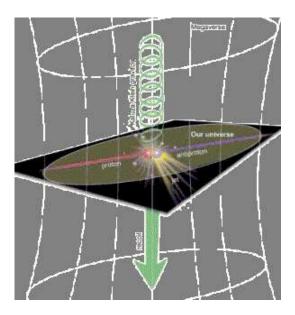
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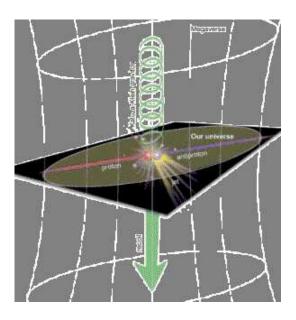
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TeV scale Brane Worlds

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Gauge hierarchy problem: Shifted towards explaining the hierarchy of compactification scales $l_t \gg l_{pl}!$

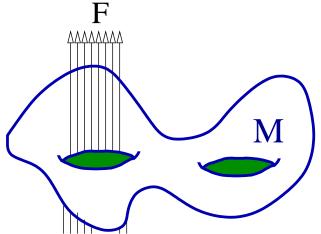
Moduli Stabilisation

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I. Background fluxes of the 10D String Theory $F_{p+1} = dC_p$:

Ex: 6D fluxes $F_p \neq 0$, yield a potential in 4D

$$V(R) = -\frac{(2-2g)}{R^4} + \frac{n^2}{R^6}$$

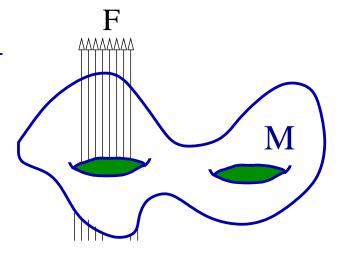


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II. Non-perturbative effects:

- String instantons generate terms of the form $V(R) = \exp(-R/g_s)$.
- Corrections to MSSM couplings like Majorana masses, Yukawa couplings, μ -terms

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The later estimate is **based** on the tree level GVW flux superpotential

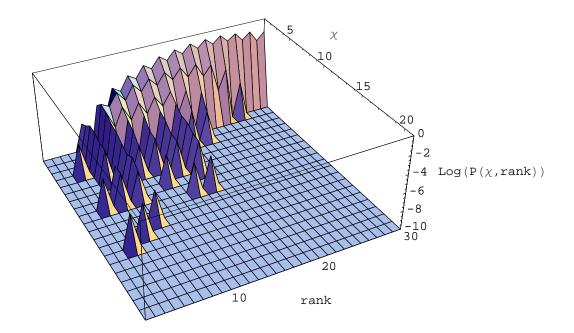
$$W = \int \Omega \wedge G$$

and G is expanded in $H^3(X)$ so that $N = L^{b_3}/b_3!$ for $L \gg b_3..$

Frequency distributions

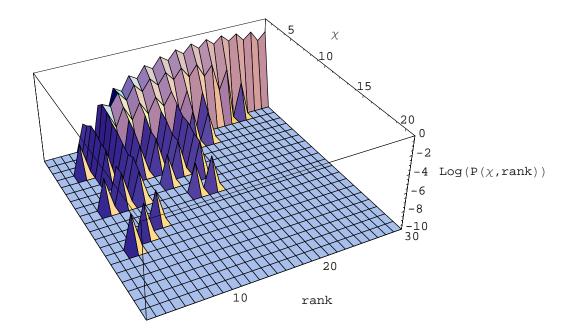
Frequency distributions

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Correlations on the landscape?

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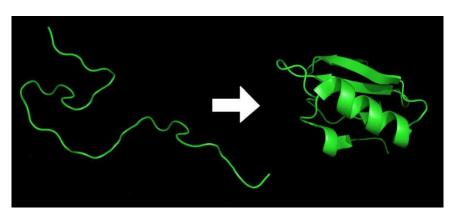
If there is really such a vast number of string vacua with different physical features in 4D, then this leads to a new view on fine tuning problems



Potential with many meta-stable minima \rightarrow Landscape of string vacua

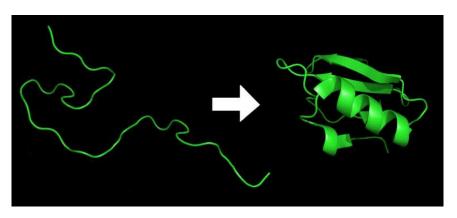
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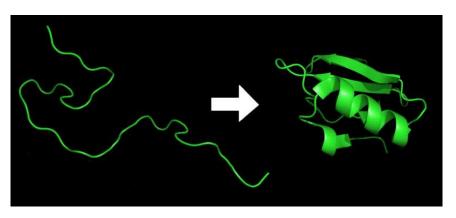
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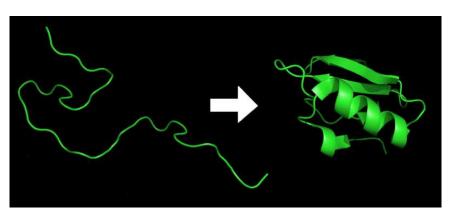


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Evolution, which might be called the A-(mino) principle

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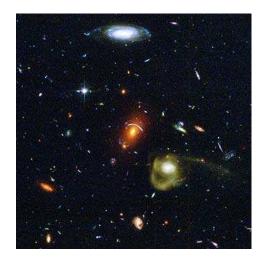
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Flatness of the universe

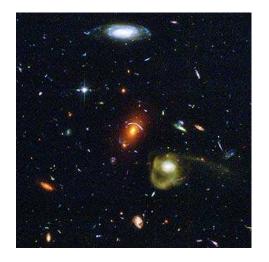


Inflation

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Inflation

Cosmological constant problem

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R + g_{\mu\nu} \Lambda = 8\pi G T_{\mu\nu}$$

No dynamical explanation yet

Fine tuning problems can in principle be solved environmentally

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However, given the accuracy with which SM parameters are measured, one can estimate that we might even get too many, like 10^{100} , vacua with acceptable 4D parameters \rightarrow predictivity?!

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(contents of Bousso's talk)

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- Statistical reasoning, entropic measure, ...
- eternal inflation, baby universes in connection with the "A-principle"

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